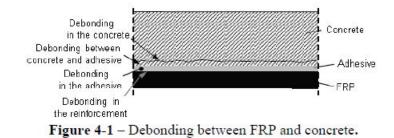
## STRENTHENING OF BEAMS AND PLATES WITH FRP (DEBONDING FAILURE MODES)



(3)P Debonding failure modes for laminates or sheets used for flexural strengthening may be classified in the following four categories, schematically represented in Figure 4-2.

- Mode 1 (Laminate/sheet end debonding)
- Mode 2 (Intermediate debonding, caused by flexural cracks)
- Mode 3 (Debonding caused by diagonal shear cracks)
- Mode 4 (Debonding caused by irregularities and roughness of concrete surface)

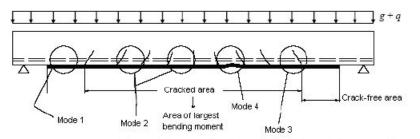


Figure 4-2 - FRP flexural strengthening: debonding failure modes

## **STRENGTHENING OF BEAMS AND PLATES WITH FRP.**

According to the Greek Code for Intervention on Existing Structures (KAN.E $\Pi$ E), the FRP reinforcement is calculated so that, in cooperation with the existing steel reinforcement, they can undertake the tension forces from required moment. As an initial approximation, the required FRP reinforcement area A<sub>j</sub>, can be calculated from:

$$A_{j} = \frac{\Delta M_{d0}}{z^{*}\sigma_{jd}} \tag{1}$$

Where:

 $\Delta M_{d0}$  is the additional moment to be carried by the strengthened section (in addition to the  $M_{d0}$  that can be undertaken by the unstrengthened section),

z can be taken as  $0.9d_j$ , where  $d_j$  is the distance of reinforcement from the outer fiber of the beam. The design value of  $\sigma_{jd}$  for the FRP should be less than the  $\sigma_{jd}$  that corresponds to either ...... of the following two types of failure:

## 1. Failure of the reinforcing material (FRP)

$$\sigma_{jd} = \frac{1}{\gamma_m} * f_{jk}$$
(2)

where:

- $f_{jk}$ :  $\eta$  characteristic tensile strength of FRP
- $\gamma_m$  =1,2 partial safety factor for the FRP.

When more than one layers of material are used, the strength is consider to be  $f'_{jk}=\psi f_{jk}$  where  $\psi$  is a reduction factor accounting for the multi-layer effect with  $\psi=1$  for n<4 and  $\psi=n^{-1/4}$ , where n is the number of the layers.

## 2. Bond failure because of insufficient anchorage length

In this case:

$$\sigma_{jd} = \frac{\sigma_{j,crit}}{\gamma_{Rd}}$$
(3)

where:

 $\gamma_{Rd}$ = 1,2 proper safety factor accounting for uncertainties in the modelling

 $\sigma_{j,\text{crit}}\text{=}$  debording shear stress

For this failure type, one may use the following relationships:

$$\sigma_{j,crit} = \beta * \frac{\tau_b^{\alpha \pi \sigma \kappa}}{t_j} * L_e$$
(4)

where  $\beta = \beta_w \beta_L$ , is a correction factor,

 $\tau_b^{\alpha\pi\sigma\kappa}=f_{ctm}$ ,

 $L_e$  is the effective bond length. The maximum value of  $L_e$  is given by:

$$L_e = \sqrt{\frac{E_j * t_j}{2 * f_{ctm}}} (MPa, mm)$$
(5)

where  $t_j, E_j$  is the thickness and the modulus of elasticity of the FRP, respectively. For more than one layers, the equivalent thickness  $t_j$  is calculated from  $t_j=\psi kt_{j1}$ , where k is the number of layers and  $\psi$  is the reduction factor, as given before.

The  $b_w$  expressing the effect of the FRP width is given by:

$$\beta_{w} = \sqrt{\frac{2 - \frac{b_{j}}{b_{w}}}{1 + \frac{b_{j}}{b_{w}}}}$$

(6)

Where  $b_j$  is the FRP width and  $b_w$  is the total width of the strengthened structural element.

The  $\beta_{L}$  expressing the effect of provided anchorage length is given by:

$$\beta_L = \sin(\frac{\pi^* \lambda}{2}) = \lambda^* (2 - \lambda) \tag{8}$$

where  $\lambda = \frac{L_{av}}{L_e} < 1$  and  $L_{av}$  is the provided length to anchor the FRP .For  $\lambda \ge 1$  coefficient  $\beta_L$  is taken as equal to 1.